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# THE FRACTAL KINETICS OF POLYMERIZATION CATALYZED BY NANOFILLERS (PART 3)

Keywords: polymerization, kinetics, catalyst, nanofiller, fractal analysis, strange diffusion.

The fractal analysis of polymerization kinetics in nanofiller presence was performed. The influence of catalyst structural features on chemical reaction course was shown. The notions of strange (anomalous) diffusion conception was applied for polymerization reactions description.

Ключевые слова: полимеризация, кинетика, катализатор, нанонаполнитель, фрактальный анализ, аномальная диффузия.

Был выполнен фрактальный анализ кинетики полимеризации в присутствии нанонаполнителя. Было показано влияние структурных особенностей катализатора на ход химической реакции. Понятие странной (аномальной) диффузии было использовано для описания реакций полимеризации.

### Introduction

By Sergeev's definition the nanochemistry is a science field connected with obtaining and studying of physical-chemical properties of particles having sizes of nanometer scale. Let's note that according to this definition polymers synthesis is automatically a nanochemistry part as far as according to the Melikhov's classification polymeric macromolecules (more precisely macromolecular coils) belong to nanoparticles and polymeric sols and gels – to nanosystems. Catalysis on nanoparticles is one of the most important sections of nanochemistry.

The majority of catalytic systems are nanosystems. At heterogeneous catalysis the active substance is tried to deposit on carrier in nanoparticles form in order to increase their specific surface. At homogeneous catalysis active substance molecules have often in them selves nanometer sizes. The most favourable conditions for homogeneous catalysis are created when reagent molecules are adsorbed rapidly by nanoparticles and are desorbed slowly but have high surface mobility and, consequently, high reaction rate on the surface and at the reaction molecules of such structure are formed at which desorption rate is increased sharply. If these conditions are realized in nanosystem with larger probability than in macrosystem, then nanocatalyst has the raising activity that was observed for many systems. In the connection such questions arise as adsorption and desorption rate, surface mobility of molecules and characteristics frequency of reagents interaction acts depend on the size, molecular relief and composition of nanoparticles and the carrier.

The presence paper purpose it the application of fractal analysis for description of polymerization kinetics in nanofiller presence.

## **Results and Discussion**

In previous parts of the article the solid-state imidization reactions were represented [1] and the interfacial interactions problems were considered [2].

As it is known [3, 4], a macromolecular coil in various polymer's states (solution, melt, solid phase) presents itself the fractal object characterized by fractal (Hausdorff) dimension  $D_f$ . Specific feature of fractal objects is the distribution of their mass in space: the

density  $\rho$  of such object changes at its radius R variation as follows [5]:

$$\rho = \rho_{dens} \left(\frac{R}{a}\right)^{D_f - d},\tag{1}$$

where  $\rho_{dens}$  is the density of material, which consists of fractal object in dense packing assumption, a is a lower linear scale of object fractal behaviour, d is the dimension of Euclidean space, in which fractal is considered (it is obvious, that in our case d=3).

From the equation (1)  $\rho$  decrease at  $D_f$  reduction follows, since it's always  $D_f < d$ , that, naturally, simplifies reagents access in macromolecular coil internal regions and results to the fuller chemical transformations, i.e. to conversion degree Q<sub>lim</sub> increase. Besides, it is known [5] that at macromolecular coil formation by irreversible aggregation mechanisms in its central part densely-packed region is formed where the proceeding of reaction is impossible. Proceeding from that, it is possible to confirm, that for a chemical reaction only a part of macromolecular coil is accessible, which is the larger, the smaller its fractal dimension  $D_f$  is. In the transparent coil case ( $D_f \le 1.5$  [3]) both low- and highmolecular substances can pass freely through it and this assumes, that in such case the value  $Q_{lim}=1.0$ . At  $D_f=2.5$ chemical reaction ceases and gelation process begins [6, 7]. This means, that at reaching  $D_f=2.5$   $Q_{lim}=0$ . The indicated estimations allow to write the fractional exponent  $v_f$  for chemical reactions similarly to the definition, accepted in paper [8]:

$$v_f = D_f - (D_f^{gel} - 1) = D_f - 1.5,$$
 (2)

where  $D_f^{gel}$  is the value  $D_f$  at gelation, equal to 2.5.

Let's remind, that according to [9], the value  $v_f$  characterizes the system states fraction unchanging in its evolution process. In case of chemical reactions generally and imidization process particularly this assumes, that the value  $v_f$  characterizes the macromolecular coil part inaccessible for chemical transformations. Then the coil part  $\beta_{ac}$  accessible for such transformations is determined as follows [10]:

$$\beta_{ac} = 1 - v_f = 2.5 - D_f. \tag{3}$$

Proceeding from the said above, it's possible to define the limiting conversion degree  $Q_{lim}$  by the following identity [10]:

$$Q_{\lim} = \beta_{ac} \,. \tag{4}$$

Therefore, the estimation  $Q_{lim}$  brings to the question of fractal dimension  $D_f$  determination. As it was noted above, at present two methods of indicated dimension determination exist. The first method consists of using chemical reactions fractal kinetics general relationship, i.e. the equation (12) [1]. Besides, the calculation of dimension  $D_f$  allows to have the equation (5) [1].

Plotting the dependences Q(t) in log-log coordinates allows to determine the value  $D_f$  according to the slope of these dependences in their linearity case according to the equation (12) [1]. In Fig. 1 the mentioned dependences for process of PAA imidization without nanofiller are shown. As one can see, these dependences are linear, that allows to make estimation  $D_f$  by the indicated method.

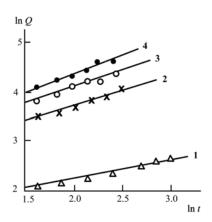


Fig. 1 - The dependences of imidization degree Q on reaction duration t in log-log coordinates for PAA imidization process at temperatures: 423 (1), 473 (2), 503 (3) and 523K (4) [11]

In Fig. 2 the comparison of the dimensions  $D_f$  calculated by two methods ( $D_{f1}$  and  $D_{f2}$ , respectively) is shown. As one can see, both methods give close values  $D_f$  and therefore further their average magnitude will be used, i.e.  $D_f = (D_{f1} + D_{f2})/2$ .

Further the parameter  $\beta_j$  can be estimated according to the equation (3) and compared with the limiting conversion degree  $Q_{lim}$ , obtained experimentally [12]. Such comparison for PAA imidization process without nanofiller and in the presence of 2 mass.% of Na<sup>+</sup>-montmorillonite at four temperatures of imidization indicated above is shown in Fig. 3 good enough correspondence of theory and experiment (their average discrepancy is equal to  $\sim$  12 %) was obtained, that confirms the offered treatment correctness [11].

Hence, the data stated above assume, that limiting conversion (in the given case – imidization) degree is defined by purely structural parameter – macromolecular coil fraction, subjected to the evolution (transformation) in chemical reaction course. This fraction can be correctly estimated within the framework of fractal analysis. For this purpose two methods of macromolecular coil fractal dimension calculation have been offered, which give coordinated results.

It is known, that the majority of catalytic systems are nanosystems [13]. At the heterogeneous catalysis active substance is being tried to deposite on the carries in nanoparticles form in order to increase their specific surface. At homogeneous catalysis active substance molecules have often by them selves nanometer sizes. It is known too [12] that the operating properties of heterogeneous catalyst systems depend on their geometry and structure of surface, which can influence strongly on catalytic properties, particularly, on catalysis selectivity. It was shown [14] that the montmorillonite surface is a fractal object. Proceeding from this, the authors [15] studied the montmorillonite fractal surface effect on its catalytic properties in isomerization reaction.

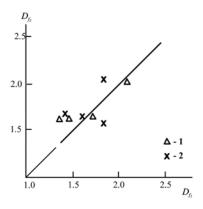


Fig. 2 - The comparison of macromolecular coil fractal dimension  $D_{f1}$  and  $D_{f2}$  calculated according to the relationships (12) and (5) [1], respectively, for PAA imidization process without filler (1) and in the presence of 2 mass.% of Na<sup>+</sup>-montmorillonite (2) [11]

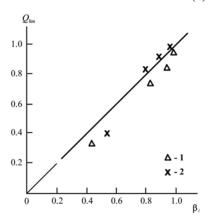


Fig. 3 - The dependence of limiting imidization degree  $Q_{lim}$  on parameter  $\beta_j$  value for PAA imidization process without nanofiller (1) and in the presence of 2 mass.% of Na<sup>+</sup>-montmorillonite (2) [11]

In paper [15] two types of montmorillonite were used – Na- montmorillonite (SW) and Ca- montmorillonite (ST). The indicated types of layered silicate were applied as a catalyst at isomerization of 1-butene (B) by obtaining of cis-2-butene (C) and trans-2-butene (T).

Meakin [9] considered the simplest catalysis scheme, which was used later for estimation of catalyst selectivity  $S_c$ . It demonstrates general features, inherent

to all catalysis models, and is expressed by a simple reaction scheme, which by analogy with the reactions (2.16)-(2.21) can be written as follows [16]:

$$A + P \to A_a, \tag{5}$$

$$A \xrightarrow{k_1} B,$$

$$A + A_a \xrightarrow{k_2} C,$$
(6)

$$\mathbf{A} + \mathbf{A}_a \xrightarrow[(cat)]{k_2} \mathbf{C},\tag{7}$$

where the reaction (5) presents itself molecule A adsorption on catalyst surface P. The reaction (6) presents itself unimolecular process, transformating adsorbed molecule A(Aa) in new molecule B, which is assumed as fastly leaving the catalyst surface. In real systems this can be an isomerization reaction (as in the considered case) or a reaction of secondary products decay. The reaction (7) presents itself molecule A addition to catalyst surface in the site already, occupied by the adsorbed molecule  $A(A_a)$  with subsequent reaction of molecule C formation, which is also assumed by fastly leaving this surface in order to make the model maximally simple. The selectivity  $S_c$  is determined as molecules C number, divided on molecules B number [17].

Within the framework of this model with using computer simulation the following expression for  $S_c$ was obtained [17]:

$$S_{c} = \frac{k_{f} \Sigma_{i} P_{i}^{2} / (k_{1} + 2P_{i}k_{f})}{k_{1} \Sigma_{i} P_{i} / (k_{1} + 2P_{i}k_{f})},$$
 (8)

where  $k_f$  is molecules A receiving rate on catalyst surface,  $P_i$  is contact probability for *i*-th site of the indicated surface.

The equation (8) is simplified essentially for two limiting cases. In the large  $k_1$  limit it accepts the form [17]:

$$S_c = \frac{k_f}{k_c} \Sigma_i P_i^2, \tag{9}$$

and in the small  $k_1$  limit let's obtain the equation

$$S = \frac{k_f}{Nk_1},$$

in which general number of surface sites N can be estimated according to the following general fractal relationship [18]:

$$N \sim L^{d_{surf}}$$
, (10)

where L is characteristic size of nanofiller particle, accepted equal to 100 nm [12],  $d_{surf}$  is catalyst surface fractal dimension.

In its turn,  $d_{surf}$  value can be estimated with the help of the relationship [19]:

$$S_u = 410 \left(\frac{L}{2}\right)^{d_{surf}-d},\tag{11}$$

where  $S_u$  is a specific surface of nanofiller particles, dis dimension of Euclidean space, in which fractal is considered (it is obvious, that in our case d=3). The value  $S_u$  is given in m<sup>2</sup>/g and L – in nm.

In Fig. 4 the dependence  $S_c(N)$  is adduced for the two types of the studied catalyst – montmorillonite. In case of 1-butene isomerization reaction the equations (5)-(7) can be written as follows [16]:

$$B + P \rightarrow B_a$$
, (12)

$$B_a \xrightarrow[(cat)]{k_1} C, \tag{13}$$

$$B + B_a \xrightarrow[(cat)]{k_2} T, \tag{14}$$

and then the value  $S_c$  is defined as the ratio T/C.

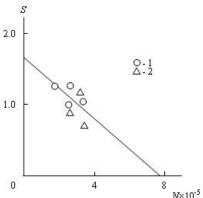


Fig. 4 - The dependence of the catalyst selectivity  $S_c$ on its surface sites general number N for Na- montmorillonite (1) and Ca-montmorillonite (2) [16]

From Fig. 4 data  $S_c$  linear decrease at Ngrowth follows. According to the equation (5) this assumes isomerization reaction course at small  $k_1$  and at fulfillment of the conditions  $k_1$ =const,  $k_f$ =const or  $k_1/k_1$ =const. In case of larger  $k_1$  (the equation (9))  $\sum_{i} P_{i}^{2} > 1/N$  [17]. For Witten-Sander clusters the value  $\sum_{i} P_{i}^{2}$  is scaled as follows [17]:

$$\Sigma_i P_i^2 \sim N^{-\gamma} \,, \tag{15}$$

where the exponent  $\gamma$  varies within the limits 0.5-0.8 [17].

One of the fractal analysis merits is a clear definition of limiting values of its main characteristics fractal dimensions. So, the value  $d_{surf}$  changes within the limits  $2 \le d_{surf} \le 3$  [20]. At  $d_{surf} = 2.0$  the value  $N=0.1\times10^5$  relative units and according to the Fig. 4 plot maximal value  $S_c$ =1.65. At maximal for real solids dimension  $d_{surf}$ =2.95 [21] N=7.94×10<sup>5</sup> of relative units and according to Fig. 4 plot  $S_c \rightarrow 0$ . This means that at such conditions trans-2-butene conversion degree goes to zero.

It was found out d<sub>surf</sub> increase results to the decrease of trans-2-butene and cis-2-butene general conversion degree. This is explained by the fact that the formed in synthesis process polymeric chain has finite rigidity and consists of statistical segments of finite length. In virtue of this circumstance it can not "repeat" the growing catalyst surface roughness at  $d_{surf}$  increase and "perceive" it as still smoother surface. In this case the effective fractal dimension of montmorillonite surface  $d_{surf}^{ef}$  is determined as follows [22]:

$$d_{surf}^{ef} = d_{surf}, (16)$$

within the interval  $d_{surf}$ =2.0-2.5 and according to the equation (16) [2] (at  $d_{surf}$  =  $d_{surf}$  and  $d_{surf}$  =  $d_{surf}$  0 within the interval 2.5-3.0.

For the studied catalysts the values  $d_{surf}=2.637$ -2.776. In Fig. 5 the dependence  $Q(d_{surf}^{ef})$  is adduced, which turns out to be linear and is extrapolated to Q=0 at  $d_{surf}^{ef}$  =2.0 (or  $d_{surf}$ =3.0) and to Q=0 at  $d_{surf}^{ef}$  = $d_{surf}$ =2.5. Thus, the combined consideration of Figs. 4 and 5 allows to assume the catalyst optimal value  $d_{surf}$ , which is equal to 2.5. At this  $d_{surf}$  magnitude Q = 1.0 and  $S_c = 1.54$ , i.e. close to maximal value  $S_c$  for montmorillonite in the considered reaction.

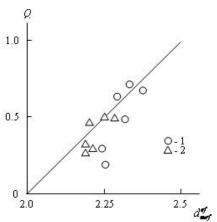


Fig. 5 - The dependence of general conversion degree Q on effective fractal dimension  $d_{surf}^{ef}$  of catalyst surface for Na- montmorillonite (1) and Ca- montmorillonite (2) [16]

Hence, the results stated above demonstrated the important role of catalyst (montmorillonite) surface fractal geometry in its catalytic properties definition [16].

Polymerization in situ (together with a filler) is often applied as a method for receiving nanocomposites. In paper [23] matrix epoxy polymer cross-linking process both in nanofiller (Na<sup>+</sup>- montmorillonite) presence and without it was studied within the framework of a strange (anomalous) diffusion conception [24]. A nanocomposites epoxy polymer/Na<sup>+</sup>- montmorillonite (EP/MMT) cross-linking was made at temperatures 353, 373 and 393K, cross-linking of EP – at 393K [25].

Let's remind the main postulates of a strange (anomalous) diffusion conception. As it is known [24], in general case diffusion processes are described according to the equation:

$$\langle r^2(t)\rangle \sim t^{\alpha},$$
 (17)

where  $\langle r^2(t) \rangle$  is mean-square displacement of a particle during time t.

If the exponent  $\alpha=1$  then the relationship (17) describes classical diffusion and if  $\alpha\neq 1$  – strange (anomalous) diffusion. Depending on concrete value  $\alpha$  persistent (superdiffusive,  $1<\alpha\leq 2$ ) and antipersistent (subdiffusive,  $0\leq \alpha<1$ ) processes are distinguished. In the strange diffusion equation the parameter  $\alpha$  has significance of "active" time fractal dimension, in which real particles walks look as random process; active time interval is proportional to  $t^{\alpha}$  [24]. In its turn, the exponent  $\beta$  in this equation [24]:

$$\frac{\alpha}{\beta} = \frac{d_s}{d} \tag{18}$$

accounts for simultaneous particles jumps ("Levy flights") from one turbulence region into another. The ratio of exponents  $\alpha/\beta$  can be determined according to the equation (18), in which spectral dimension  $d_s$  is de-

termined, in its turn, according to the relationship (2) [1].

The estimations have shown [23], that the introduction MMT in reactionary mixture increases substantially the value  $d_s$ : if for reaction without MMT  $d_s$ =0.027, then at MMT introduction  $d_s$  increases up to 0.175-0.452 and rises at cross-linking temperature increase. A macromolecular coil (microgel) fractal dimension EP  $D_f$  can be determined with the help of the relationship (12) [1] the account made according to the indicated ratio has shown, that the smallest value  $D_f$  equal to 1.52, is obtained for cross-linking reaction without MMT and at MMT introduction it increases up to 1.67-2.19.

The authors [23] have proceeded from the assumption, that the dependence Q on active time  $t^{\alpha}$  should be linear and general for all the four studied reactions. The exponent  $\beta$  value was chosen on the base of this assumption. It turns out, that  $\beta$  decreases both at MMT introduction and at the temperature raising from 28 up to 3.8. Besides, at cross-linking reaction without MMT course the decrease  $\beta$  from 28 up to 9 is observed. In Fig. 6 the dependence  $Q(t^{\alpha})$  for all the studied reactions is adduced. As one can see, the general linear correlation is obtained. The active time increases at MMT introduction: for reaction without MMT it makes  $\sim 2\%$  from the real one and at MMT presence it can reach 30%.

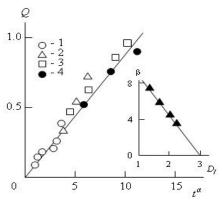


Fig. 6 - The dependence of cross-linking degree Q on active time  $t^{\alpha}$  for reaction without MMT (1) and in MMT presence at T=353 (2), 373 (3) and 393K (4). In the insert: the dependence  $\beta(D_f)$  [23]

In the insert the dependence  $\beta$  on  $D_f$  is shown, from which  $\beta$  decrease at microgel fractal dimension growth follows. This assumes "Levy flights" probability decrease at the system viscosity increase. Hence, the ability to control active time gives the possibility of reaction course operation.

### **Conclusions**

Thus, the present work results have been shown the applicability and usefullness of fractal analysis and strange (anomalous) diffusion conception for description of polymerization reactions, catalyzed by nanofillers. The nanofiller introduction in reactionary mixture results in two-phase system formation, where a decisive role will be played by interfacial interactions.

The polymerization conversion degree is defined by its active (fractal) time. Hence, the ability to control active time gives the possibility of reaction course operation.

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